

Programs as Data 6

Imperative languages, environment and store, micro-C

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Today

- Course overview
- A naïve imperative language
- C concepts
 - Pointers and pointer arithmetics, arrays
 - Lvalue and rvalue
 - Parameter passing by value and by reference
 - Expression statements
- Micro-C, a subset of C
 - abstract syntax
 - lexing and parsing
 - interpretation

The overall course plan

- F# and functional programming
- Interpreting an expression language
- Lexing and parsing tools
- Interpreting a functional language, micro-ML
 - Higher-order functions
- Type checking and type inference
- Interpreting an imperative language, micro-C
- Compiling micro-C to stack machine code
- Real-world abstract machines: JVM and .NET
 - Garbage collection techniques
- Continuations, exceptions and backtracking
- (Programs that generate programs, Scheme)
- Or maybe Scala, a functional/OO language on JVM

A naive-store imperative language

- **Naive** store model:
 - a variable name maps to an integer value
 - so store is just a runtime environment

```
sum = 0;  
for i = 0 to 100 do  
    sum = sum + i;
```

i	100
sum	5050

```
i = 1;  
sum = 0;  
while sum < 10000 do begin  
    sum = sum + i;  
    i = 1 + i;  
end;
```

i	142
sum	10011

Naïve-store statement execution, 1

- Executing a statement gives a new store
- Assignment $x=e$ updates the store
- Expressions do not affect the store

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | Asgn(x, e) ->  
    setSto store (x, eval e store)  
  | If(e1, stmt1, stmt2) ->  
    if eval e1 store <> 0 then exec stmt1 store  
    else exec stmt2 store  
  | ...
```

Update store
at x with
value of e

Naïve-store statement execution, 2

- A block $\{s_1; \dots; s_n\}$ executes s_1 then $s_2 \dots$
- Example:

```
exec (Block [s1; s2]) store
= loop [s1; s2] store
= exec s2 (exec s1 store)
```

```
let rec exec stmt (store : naivestore) : naivestore =
  match stmt with
  | Block stmts ->
    let rec loop ss sto =
      match ss with
      | [] -> sto
      | s1::sr -> loop sr (exec s1 sto)
    loop stmts store
  | ...
```

Naïve-store statement execution, 3

- **for** and **while** update the store sequentially

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | ...  
  | For(x, estart, estop, stmt) -> ...  
  | While(e, stmt) ->  
    let rec loop sto =  
      if eval e sto = 0 then sto  
        else loop (exec stmt sto)  
    loop store
```

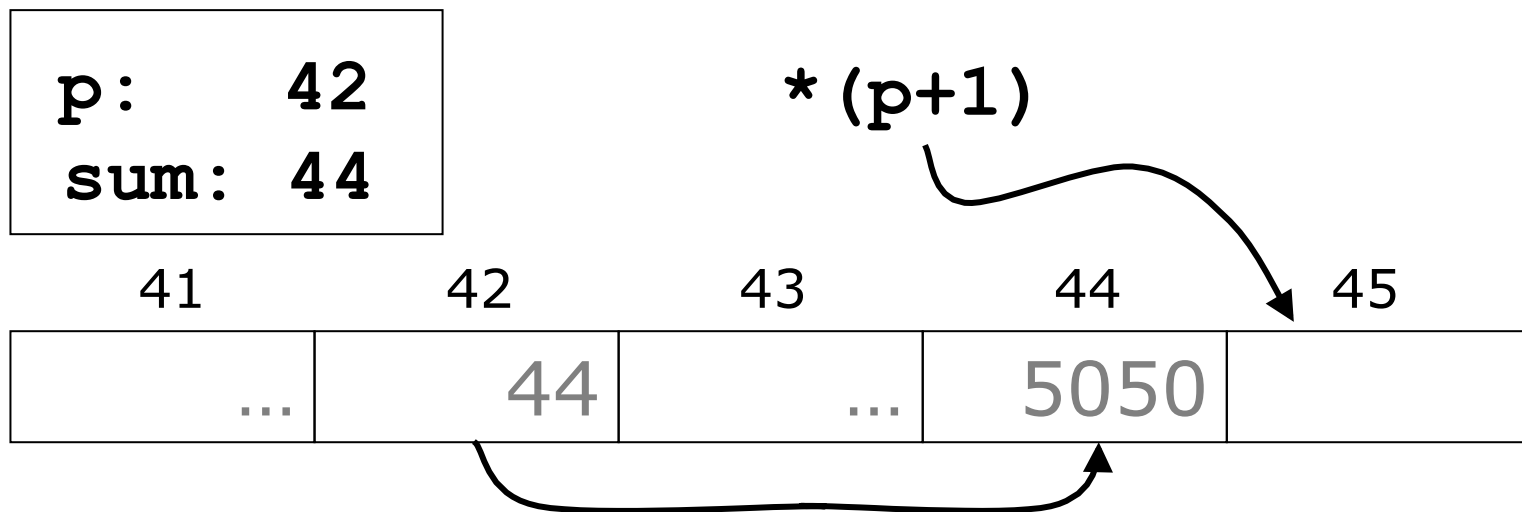
Environment and store, micro-C

- The naive model cannot describe *pointers* and *variable aliasing*
- A more realistic store model:
 - *Environment* maps a variable name to an address
 - *Store* maps address to value



The essence of C: Pointers

- Main innovations of C (1972) over Algol 60:
 - Structs, as in COBOL and Pascal
 - Pointers, pointer arithmetics, pointer types, array indexing as pointer indexing
 - Syntax: { } for blocks, as in C++, Java, C#



- Very different from Java and C#, which have no pointer arithmetics, but garbage collection

Desirable language features

	C	C++	F#/ML	Smtalk	Haskell	Java	C#
Garbage collection	Red	Red	Green	Green	Green	Green	Green
Exceptions	Red	Green	Green	Green	Red/Green diagonal	Green	Green
Bounds checks	Red	Red	Green	Green	Green	Green	Green
Static types	Red	Green	Green	Red	Green	Green	Green
Generic types (para. polym.)	Red	Red/Green diagonal	Green	Red	Green	Green	Green
Pattern matching	Red	Red	Green	Red	Green	Red	Red
Reflection	Red	Red	Light Green	Green	Red	Green	Green
Refl. on type parameters	Red	Red	Light Green	Red	Red	Red	Green
Anonymous functions (λ)	Red	Red	Green	Green	Green	Red/Green diagonal	Green
Streams	Red	Red	Light Green	Red	Green	Red	Red/Green diagonal
Lazy eval.	Red	Red	Light Green	Red	Green	Red	Red

C pointer basics

- A pointer p refers to a storage location
- The dereference expression $*p$ means:
 - *the content of the location* (rvalue) as in
 $*p + 4$
 - *the storage location itself* (lvalue), as in
 $*p = x+4$
- The pointer that points to x is $\&x$
- Pointer arithmetics:
 - $*(p+1)$ is the location just after $*p$
- If p equals $\&a[0]$
then $*(p+i)$ equals $p[i]$ equals $a[i]$,
so an array is a pointer
- Strange fact: $a[2]$ can be written $2[a]$ too

Using pointers for return values

- Example ex5.c, computing square(x):

```
void main(int n) {  
    ...  
    int r;  
    square(n, &r);  
    print r;  
}  
  
void square(int i, int *rp) {  
    *rp = i * i;  
}
```

for input

for return value: a
pointer to where to
put the result

Recursion and return values

- Computing factorial with MicroC/ex9.c

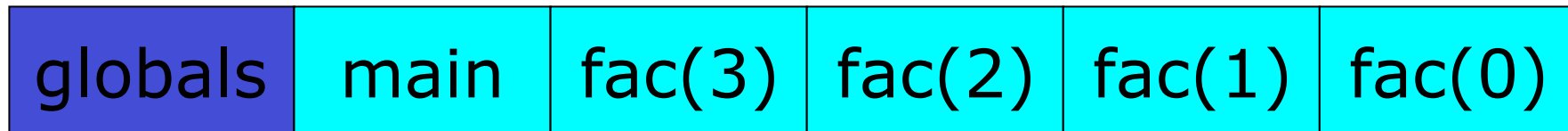
```
void main(int i) {
    int r;
    fac(i, &r);
    print r;
}

void fac(int n, int *res) {
    if (n == 0)
        *res = 1;
    else {
        int tmp;
        fac(n-1, &tmp);
        *res = tmp * n;
    }
}
```

- **n** is input parameter
- **res** is output parameter: a pointer to where to put the result
- **tmp** holds the result of the recursive call
- **&tmp** gets a pointer to **tmp**

Storage model for micro-C

- The store is an indexable stack
 - Bottom: global variables at fixed addresses
 - Plus, a stack of activation records



- An *activation record* is an executing function
 - return address and other administrative data
 - parameters and local variables
 - temporary results



Lvalue and rvalue of an expression

- Rvalue is “normal” value, right-hand side of assignment: `17`, `true`
- Lvalue is “location”, left-hand side of assignment: `x`, `a[2]`
- In assignment `e1=e2`, expression `e1` must have lvalue

- Where else must an expression have lvalue in C#? In C?

	Has lvalue	Has rvalue
<code>x</code>	yes	yes
<code>a[2]</code>	yes	yes
<code>*p</code>	yes	yes
<code>x+2</code>	no	yes
<code>&x</code>	no	yes

Call-by-value and call-by-reference, C#

```
int a = 11;  
int b = 22;  
swapV(a, b);  
swapR(ref a, ref b);
```

a: 41
b: 42

addresses

by value

```
static void swapV(int x, int y) {  
    int tmp = x; x = y; y = tmp;  
}
```

x: 43
y: 44
tmp: 45

by reference

```
static void swapR(ref int x, ref int y) {  
    int tmp = x; x = y; y = tmp;  
}
```

x: 41
y: 42
tmp: 43

41 42 43 44 45

store

11	22	22	11	11
----	----	----	----	----

C variable declarations

Declaration	Meaning
int n	n is an integer
int *p	p is a pointer to integer
int ia[3]	ia is array of 3 integers
int *ipa[4]	ipa is array of 4 pointers to integers
int (*iap)[3]	iap is pointer to array of 3 integers
int *(*ipap)[4]	ipap is pointer to array of 4 pointers to ints

Unix program `cdecl` or www.cdecl.org may help:

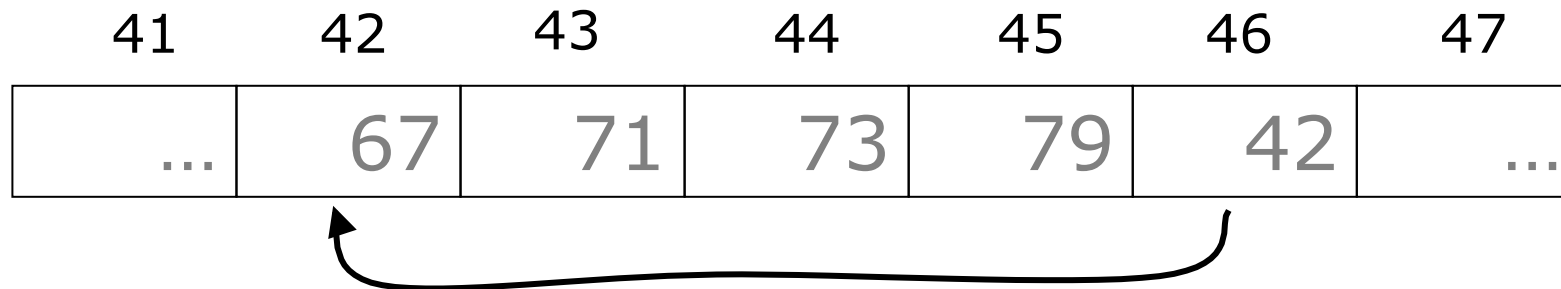
```
cdecl> explain int *(*ipap)[4]
declare ipap as pointer to array 4 of pointer to int
cdecl> declare n as array 7 of pointer to pointer to int
int **n[7]
```

Micro-C array layout

- An array `int arr[4]` consists of

- its 4 int elements
- a pointer to `arr[0]`

`arr: 46`



- This is the uniform array representation of B
- Real C treats array parameters and local arrays differently; complicates compiler
- Strachey's CPL -> Richards's BCPL -> B -> C

Micro-C syntactic concepts

- Types

<code>int</code>	<code>TypI</code>
<code>int *x</code>	<code>TypP (TypI)</code>
<code>int x[4]</code>	<code>TypA (TypI, Some 4)</code>

- Expressions

`(*p + 1) * 12`

- Statements

`if (x!=0) y = 1/x;`

- Declarations

– of global or local variables

`int x;`

– of global functions

`void swap(int *x, int *y) { ... }`

Micro-C abstract syntax

type typ =			
TypI	(* Type int		*)
TypC	(* Type char		*)
TypA of typ * int option	(* Array type		*)
TypP of typ	(* Pointer type		*)
and expr =			
Access of access	(* x or *p or a[e]		*)
Assign of access * expr	(* x=e or *p=e or a[e]=e		*)
Addr of access	(* &x or &*p or &a[e]		*)
CstI of int	(* Constant		*)
Prim1 of string * expr	(* Unary primitive operator		*)
Prim2 of string * expr * expr	(* Binary primitive operator		*)
Andalso of expr * expr	(* Sequential and		*)
Orelse of expr * expr	(* Sequential or		*)
Call of string * expr list	(* Function call f(...)		*)
and access =			
AccVar of string	(* Variable access	x	*)
AccDeref of expr	(* Pointer dereferencing	*p	*)
AccIndex of access * expr	(* Array indexing	a[e]	*)
and stmt =			
If of expr * stmt * stmt	(* Conditional		*)
While of expr * stmt	(* While loop		*)
Expr of expr	(* Expression statement	e;	*)
Return of expr option	(* Return from method		*)
Block of stmtordec list	(* Block: grouping and scope		*)
and stmtordec =			
Dec of typ * string	(* Local variable declaration		*)
Stmt of stmt	(* A statement		*)
and topdec =			
Fundec of typ option * string * (typ * string) list * stmt			
Vardec of typ * string			
and program =			
Prog of topdec list			

Types

rvalue

Expressions

lvalue

Statements

Declarations

Lexer specification for micro-C

- New: endline comments `// blah blah`
and delimited comments `if (x /* y? */)`

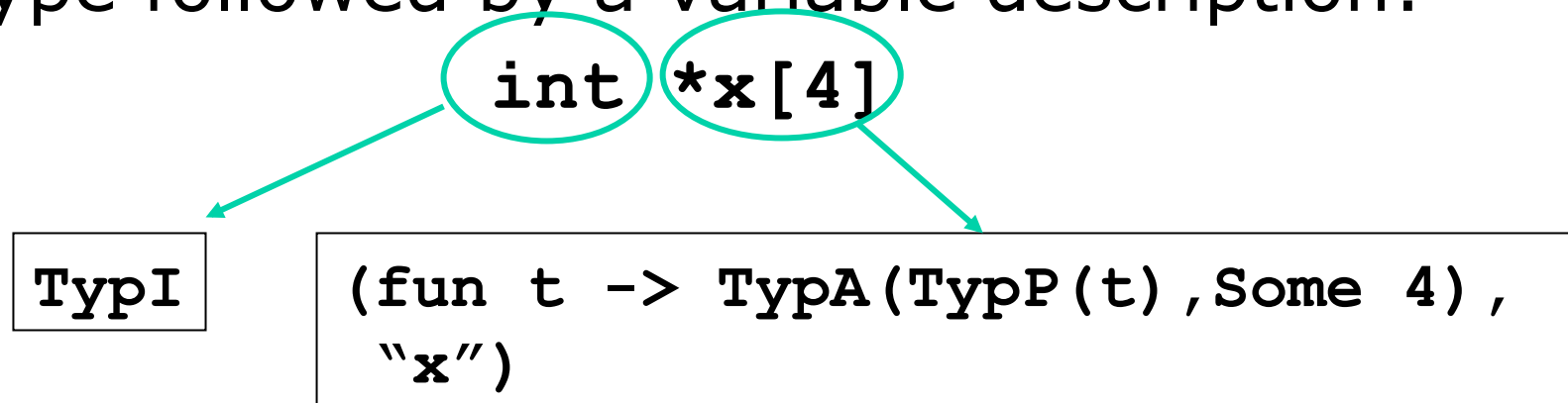
```
rule Token = parse
| ...
| "//"          { EndLineComment lexbuf; Token lexbuf }
| "/*"         { Comment lexbuf; Token lexbuf }
```

```
and EndLineComment = parse
| ['\n' '\r']   { () }
| (eof | '\026') { () }
| _            { EndLineComment lexbuf }
```

```
and Comment = parse
| "/*"         { Comment lexbuf; Comment lexbuf }
| "*/"         { () }
| ['\n' '\r']   { Comment lexbuf }
| (eof | '\026') { lexerError lexbuf "Unterminated" }
| _            { Comment lexbuf }
```

Parsing C variable declarations

- Hard, declarations are *mixfix*: `int *x[4]`
- Parser trick: Parse a variable declaration as a type followed by a variable description:



- Parse var description to get pair (\mathbf{f}, \mathbf{x}) of type function \mathbf{f} , and variable name \mathbf{x}
- Apply \mathbf{f} to the declared type to get type of \mathbf{x}
`Vardec (TypA (TypP (TypI) , Some 4) , "x")`

Interpreting micro-C

- Interpreter data:
 - *locEnv, environment* mapping local variable names to store addresses
 - *gloEnv, environment* mapping global variable names to store addresses, and global function names to (parameter list, body statement)
 - *store*, mapping addresses to (integer) values
- Main interpreter functions:
 - exec: `stmt -> locEnv -> gloEnv -> store -> store`
 - eval: `expr -> locEnv -> gloEnv -> store -> int * store`
 - access: `access -> locEnv -> gloEnv -> store -> address * store`

Micro-C statement execution

- As for the naïve language, but two envs:

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  | If(e, stmt1, stmt2) ->  
    let (v, store1) = eval e locEnv gloEnv store  
    if v<>0 then exec stmt1 locEnv gloEnv store1  
    else exec stmt2 locEnv gloEnv store1  
  | While(e, body) ->  
    let rec loop store1 =  
      let (v, store2) = eval e locEnv gloEnv store1  
      if v<>0 then loop (exec body locEnv gloEnv store2)  
      else store2  
    in loop store  
  | ...
```


Expression statements in C, C++, Java and C#

- The "assignment statement"

$x = 2+y;$

is really an expression

$x = 2+y$

followed by a semicolon

Value: none
Effect: change x

Value: $2+y$
Effect: change x

- The semicolon means: ignore value

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  | ...  
  | Expr e ->  
    let (_, store1) = eval e locEnv gloEnv store  
    store1
```

Evaluate expression
then ignore its value

Micro-C expression evaluation, 1

- Evaluation of an expression
 - takes local and global env and a store
 - gives a resulting *rvalue* and a *new store*

```
and eval e locEnv gloEnv store : int * store =
  match e with
  | ...
  | CstI i          -> (i, store)
  | Prim2(ope, e1, e2) ->
    let (i1, store1) = eval e1 locEnv gloEnv store
    let (i2, store2) = eval e2 locEnv gloEnv store1
    let res =
      match ope with
      | "*"  -> i1 * i2
      | "+"  -> i1 + i2
      | ...
    (res, store2)
```

Micro-C expression evaluation, 2

- To evaluate access expression **x**, ***p**, **arr[i]**
 - find its lvalue, as an address **loc**
 - look up the rvalue in the store, as **store1[loc]**
- To evaluate **&e**
 - just evaluate **e** as lvalue
 - return the lvalue

rvalue

```
and eval e locEnv gloEnv store : int * store =  
  match e with  
  | Access acc ->  
    let (loc, store1) = access acc locEnv gloEnv store  
    (getSto store1 loc, store1)  
  | Addr acc -> access acc locEnv gloEnv store  
  | ...
```

Micro-C access evaluation, to *lvalue*

- A variable **x** is looked up in environment
- A dereferencing ***e** just evaluates **e** to an address
- An array indexing **arr[idx]**
 - evaluates **arr** to address **a**, then gets **aval=store[a]**
 - evaluates **e** to **rvalue** index **i**
 - returns address **(aval+i)**

lvalue

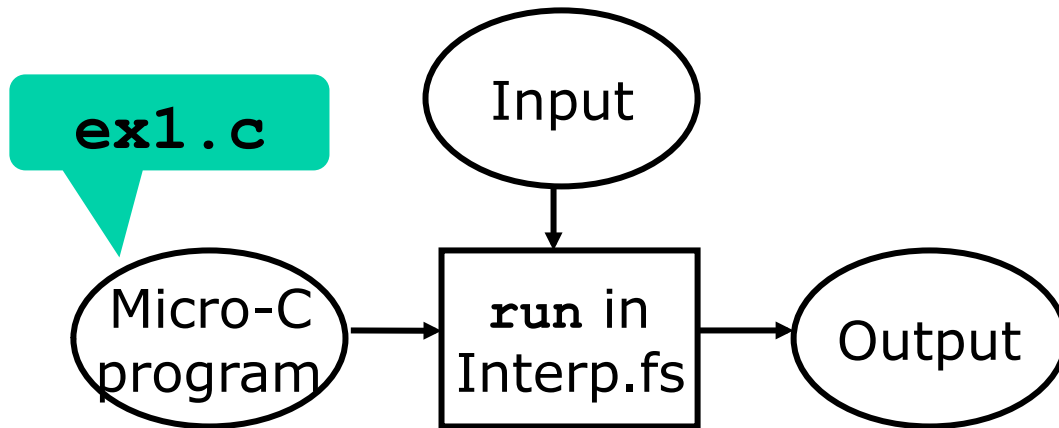
```
and access acc locEnv gloEnv store : int * store =
  match acc with
  | AccVar x          -> (lookup (fst locEnv) x, store)
  | AccDeref e        -> eval e locEnv gloEnv store
  | AccIndex(acc, idx) ->
    let (a, store1) = access acc locEnv gloEnv store
    let aval = getSto store1 a
    let (i, store2) = eval idx locEnv gloEnv store1
    (aval + i, store2)
```

Operators $\&x$ and $*p$ are inverses

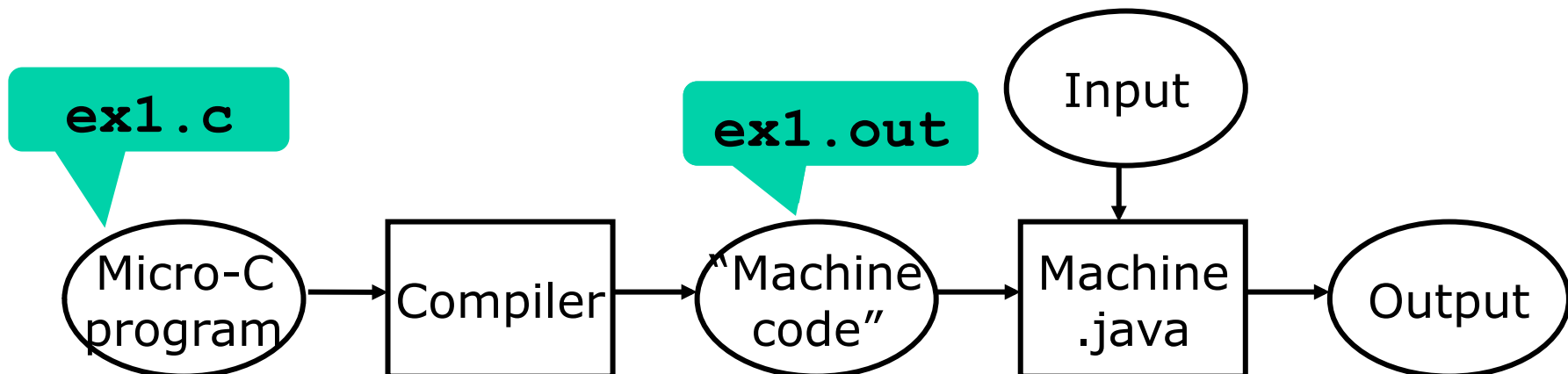
- The address-of operator $\&e$
 - evaluates e to its lvalue
 - returns the lvalue (address) as if it were an rvalue
- The dereferencing operator $*e$
 - evaluates e to its rvalue
 - returns the rvalue as if it were an lvalue
- It follows
 - that $\&(*e)$ equals e
 - that $*(\&e)$ equals e , provided e has lvalue

Micro-C, interpreter and compiler

- This lecture: Interpretation of micro-C



- Next lecture: Compilation of micro-C



Reading and homework

- This week's lecture:
 - PLCSD chapter 7
 - Strachey: Fundamental Concepts ...
 - Kernighan & Ritchie: The C programming language, chapter 5.1-5.5

- Next lecture
 - PLCSD chapter 8