CPSC 201: Introduction to Computer Science Carsten Schürmann Date: February 17, 2002

Homework 3

Due: Wednesday, February 20, 2002.

Guidelines

While we acknowledge that beauty is in the eye of the beholder, you should nonetheless strive for elegance in your code. Not every program which runs deserves full credit. Make sure to state invariants in comments which are sometimes implicit in the informal presentation of an exercise. If auxiliary functions are required, describe concisely what they implement. Do not reinvent wheels, and try to make your functions small and easy to understand. Use tasteful layout and avoid long winded and contorted code. None of the problems requires more than a few lines of SML code.

Problem 1: Speeding tickets (50 points)

A friend called you yesterday with some bad news. He got a speeding ticket on Whitney Ave. Even debating skills did not help him to convince the police to let him go. 35mph in a 25mph zone is just not acceptable, they said. This brought him to an idea, for which he needs your help. He wants to design a piece of hardware that can be set to a tempo limit and will raise an alarm signal once the current speed exceeds it. Modern cars are all computer controlled, so it should not be very difficult to get access to a digital representation of the current cruising speed.

Your friend would have used your piece of hardware in the following way. He would have set the current speed limit to 25mph and the alarm should have gone off way before the police stopped him. All you have to do now is to define a circuit that takes two 8 bit numbers as input, and returns one alarm bit as output. It is set to 1 once the first number exceeds the second.

1. Write out a truth table for a circuit that compares only two one bit numbers.

Hint: Your circuit should have two in-connectors x and y, and two out-connectors e, l, where e is true if x = y, and l is true if x < y.

- Write out a Boolean expression for the truth table in 1.
 Hint: Your truth table should have four columns relating x, y, l, and e.
- 3. Design a circuit that implements this in hardware.

Hint: This means on a piece of paper, or in ASCII.

4. Generalize the circuit to n bit numbers.

Hint: Again, draw the circuit on a piece of paper. Write out the circuit for the nth stage, the n-1th stage, and the last stage. We will be able to reconstruct the missing details.

5. Implement your circuit in the simulator we used in class.

Hint: Use the file /c/cs201/lib/code/ass3/problem1.sml which contains all necessary auxiliary functions discussed in class. Write the following functions.

```
(a) eq : Circuit -> Circuit -> Circuit (implements e, see lecture 11)
```

(b) lt : Circuit -> Circuit -> Circuit (implements *l*)

(c) comp1bit : Circuit -> Circuit -> [Circuit] (one bit comparator)

```
(d) compnbit : [Circuit] -> [Circuit] -> [Circuit] (n bit comparator)
```

To test your code, declare the three different values for the different speeds:

```
val speed23 =
  [SIGNAL 0,SIGNAL 0,SIGNAL 0,SIGNAL 1,SIGNAL 0,SIGNAL 1,SIGNAL 1]
val speed25 =
  [SIGNAL 0,SIGNAL 0,SIGNAL 0,SIGNAL 1,SIGNAL 1,SIGNAL 0,SIGNAL 0,SIGNAL 0]
val speed35 =
  [SIGNAL 0,SIGNAL 0,SIGNAL 1,SIGNAL 0,SIGNAL 0,SIGNAL 1,SIGNAL 1]
```

To test your code, compare your results with the following experiments:

simulateList (compnbit speed25 speed23);
val it = [SIGNAL 0,SIGNAL 0] : Circuit list

indicates that the speed limited has not been exceeded. The right is the alarm flag.

```
simulateList (compnbit speed25 speed35);
val it = [SIGNAL 0,SIGNAL I] : Circuit list
```

indicates that the alarm has ringing. An finally

```
simulateList (compnbit speed25 speed25);
val it = [SIGNAL I,SIGNAL 0] : Circuit list
```

shows that the alarm has not gone off yet, but that the system recognized that the vehicle is going *exactly* speed limit.

Problem 2: Machine organization (50 points)

When simulating the run of a machine, it is of utmost importance how memory is represented. In the last assignment, the choice fell on a BOOL list. This was good because it illustrated clearly how memory is organized. In this assignment, however, we want to study how memory interacts with other parts of the machine and how machine language really works. We therefore take the freedom to abstract from some details, especially, from bits and bytes and concentrate on the essence on how to address, create, update, and maintain memory.

First, we introduce the address space. We abstract from concrete addressing techniques in a real machine and define an *address* simply to be an integer.

type address = int

If we represent memory as a list of Boolean values, update is going to be very expensive. One can do better by using data structures such as balanced trees or hashtables, for quick lookup and update. For our purposes, however, it is completely sufficient to use a less efficient albeit more elegant technique to implement memory as a function from addresses to their content.

```
datatype Content
  = Free
  | Int of int
  | Real of real
type memory = address -> Content
```

Each memory cell can be either free, contain an integer or a real number. This allows us abstract away from all details covered in the previous assignment. The representation invariant behind memory is as follows. If M is of type memory, then for any valid address a, M a returns the content of M at a.

1. Define the empty memory.

empty : memory

Hint : empty 2004 should evaluate to Free.

2. Write a function that updates memory.

update : memory -> address -> Content -> memory

update M a C updates M at address a to content C.

Hint: The update function is easier to implement then you might assume. To see if it does the right thing, consider for example

val mem = update empty 2000 (Real 1.414)

which sets the content at address 2000 to Real 1.414.

3. Write a function the looks up information in memory.

lookup : memory -> address -> Content

lookup M a looks up address a in M.

Hint: Lookup is even easier to implement than update. As example consider the following command.

- lookup mem 2000; val it = Real 1.414 : Content

4. Write a function that lets the user inspect memory.

inspect : memory -> (int * int) -> unit

memory M (a, b) prints the content of memory M between addresses a and b, inclusive. For example, after storing 1.414 at address 2000, and 42 at the address 2001, inspect should provide the following output on the screen.

```
- inspect mem (2000, 2010);
2000 1.414
2001 42
2002
     *
2003
     *
2004
     *
2005
     *
2006 *
2007 *
2008 *
2009 *
2010 *
val it = () : unit
```

Hint: Use the print command.

Hand-in Instructions

In the course directory /c/cs201/bin, there are five programs that support you in submitting your solution to the homework.

```
submit assignment-number file(s)
unsubmit assignment-number file(s)
check assignment-number
protect assignment-number file(s)
unprotect assignment-number file(s)
```

submit allows you to submit one of several files. For example

/c/cs201/bin/submit 3 hw3.sml hw3-examples.sml

submits your file hw3.sml and hw3-examples.sml. check can give you the peace of mind that your solution has really been submitted, and if you would like to make last minute changes to your solution, use unsubmit before submitting the updated version. protect and unprotect give you the power to protect/unprotect submitted solutions from deletion.